



# **CARIBBEAN EXAMINATIONS COUNCIL**

## **Caribbean Secondary Education Certificate**

# **Mathematics Syllabus**

**Effective for examinations from May/June 2010**

Correspondence related to the syllabus should be addressed to:

The Pro-Registrar  
Caribbean Examinations Council  
Caenwood Centre  
37 Arnold Road, Kingston 5, Jamaica, W.I.

Telephone: (876) 920-6714  
Facsimile Number: (876) 967-4972  
E-mail Address: [cxcwzo@cxc.org](mailto:cxcwzo@cxc.org)  
Website: [www.cxc.org](http://www.cxc.org)

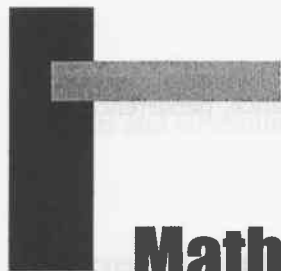
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# Mathematics Syllabus

## ◆ RATIONALE

The guiding principles of the Mathematics syllabus direct that Mathematics as taught in Caribbean schools should be *relevant to the existing and anticipated needs of Caribbean society, related to the abilities and interests of Caribbean students and aligned with the philosophy of the educational system*. These principles focus attention on the use of Mathematics as a problem solving tool, as well as on some of the fundamental concepts which help to unify Mathematics as a body of knowledge. The syllabus explains general and unifying concepts that facilitate the study of Mathematics as a coherent subject rather than as a set of unrelated topics.

*Every citizen needs basic computational skills (addition, subtraction, multiplication and division) and the ability to use these mentally to solve everyday problems. All citizens should recognize the importance of accuracy in computation as the foundation for deductions and decisions based on the results. In addition, the citizen should have, where possible, a choice of mathematical techniques to be applied in a variety of situations. A 'range of mathematical techniques' is therefore, specified in recognition of the need to accommodate different levels of ability. Citizens need to use Mathematics in many forms of decision-making: shopping, paying bills, budgeting and for the achievement of personal goals, critically evaluating advertisements, taxation, investing, commercial activities, banking, working with and using current technologies, measurements and understanding data in the media. Improving efficiency and skills in these matters will be beneficial to the community as well as to the individual.*

The syllabus seeks to provide for the needs of specific mathematical techniques in the future careers of students, for example, in agriculture and in commercial and technical fields. *By the end of the normal secondary school course, students should appreciate that the various branches of Mathematics are not rigidly segregated and that the approach to the solution of any problem is not necessarily unique.*

## ◆ AIMS

*This syllabus aims to:*

1. *help students appreciate the use of mathematics as a form of communication;*
2. *help students acquire a range of mathematical techniques and skills and to foster and maintain the awareness of the importance of accuracy;*
3. *make Mathematics relevant to the interests and experiences of students by helping them to recognize Mathematics in their environment;*
4. *cultivate the ability to apply mathematical knowledge to the solution of problems which are*

meaningful to students as citizens;

5. help students cultivate the ability to think logically and critically;
6. help students develop positive attitudes, such as open-mindedness, self-reliance, persistence and a spirit of enquiry;
7. prepare students for the use of Mathematics in further studies;
8. help students develop an appreciation of the wide application of Mathematics and its influence in the *development and* advancement of civilization;
9. help students become increasingly aware of the unifying structure of Mathematics.

## ◆ ORGANIZATION OF THE SYLLABUS

The syllabus is arranged as a set of topics, and each topic is defined by its specific objectives *and content*. It is expected that students would be able to master the specific objectives *and related content* after pursuing a course in Mathematics over five years of secondary schooling.

The design allows for a **Core** which contains selected mathematical skills, knowledge and abilities necessary for any citizen in our contemporary society as well as objectives to meet the needs of those who will be:

- (a) pursuing careers as agriculturalists, engineers, scientists, economists;
- (b) proceeding to study Mathematics at an advanced level;
- (c) engaged in the business and commercial world.

The Examination will also comprise an **Optional** section which will be defined by *additional* specific objectives.

## ◆ FORMAT OF THE EXAMINATIONS

The examination will consist of two papers: Paper 01, an objective type paper based on the **Core Objectives** and Paper 02, an essay or problem solving type paper based on *both the Core and Optional Objectives*.

Paper 01  
(1 hour 30 minutes)

**The Paper will consist of 60 multiple-choice items, sampling the Core as follows:**

Sections	No. of items
Computation	6
Number Theory	4
Consumer Arithmetic	8
Sets	4
Measurement	8
Statistics	6
Algebra	9
Relations, Functions and Graphs	6
Geometry and Trigonometry	9
<b>Total</b>	<b>60</b>

Each item will be allocated one mark.

**Paper 02**  
(2 hours and 40 minutes)

The Paper will consist of two sections.

**Section I: 90 marks**

The section will consist of 8 compulsory *structured and* problem-solving type questions based on the **Core**.

The marks allocated to the topics are:

Sections	No. of marks
Sets	5
Consumer Arithmetic and Computation	10
Measurement	10
Statistics	10
Algebra	15
Relations, Functions and Graphs	10
Geometry and Trigonometry	20
*Combination question/ investigation	<u>10</u>
<b>Total</b>	<b>90</b>

\* Combination question/investigation may be set on any combination of objectives in the **Core** including Number Theory.

**Section II: 30 marks**

This section will consist of 3 *structured or* problem-solving questions based mainly on the **Optional Objectives** of the syllabus. There will be 1 question from each of the *Sections* Algebra and Relations, Functions and Graphs; *Measurement and* Geometry and Trigonometry; and Vectors and Matrices.

Candidates will be required to answer **any two** questions. Each question will be allocated 15 marks.

The optional questions will be set as follows:

**ALGEBRA AND RELATIONS, FUNCTIONS AND GRAPHS**

The *question* in this section may be set on:

Algebra

*Optional* Specific Objective 17 or any of the other Specific Objectives in Algebra.

Relations, Functions and Graphs

*Optional* Specific Objectives 15, 22, 23, 24, 25 or any of the other Specific Objectives in Relations, Functions and Graphs.

## MEASUREMENT AND GEOMETRY AND TRIGONOMETRY

The question in this section may be set on:

### Measurement

Optional Specific Objectives 5, 6 or any of the other Specific Objectives in Measurement.

### Geometry and Trigonometry

Optional Specific Objective 20 or any of the other Specific Objectives in Geometry and Trigonometry.

## VECTORS AND MATRICES

The question in this section may be set on:

Optional Specific Objectives 5, 11, 12, 13 or any of the other Specific Objectives in Vectors and Matrices.

## ◆ CERTIFICATION AND PROFILE DIMENSIONS

The subject will be examined for certification at the General Proficiency.

In each paper, items and questions will be classified, according to the kind of cognitive demand made, as follows:

### Knowledge

Items that require the recall of rules, procedures, definitions and facts, that is, items characterized by rote memory as well as simple computations, computation in measurements, constructions and drawings.

### Comprehension

Items that require algorithmic thinking that involves translation from one mathematical mode to another. Use of algorithms and the application of these algorithms to familiar problem situations.

### Reasoning

Items that require:

- (i) translation of non-routine problems into mathematical symbols and then choosing suitable algorithms to solve the problems;
- (ii) combination of two or more algorithms to solve problems;
- (iii) use of an algorithm or part of an algorithm, in a reverse order, to solve a problem;
- (iv) the making of inferences and generalizations from given data;
- (v) justification of results or statement;
- (vi) analyzing and synthesizing.

Candidates' performance will be reported under Knowledge, Comprehension and Reasoning that are roughly defined in terms of the three types of demand.

## WEIGHTING OF PAPER AND PROFILE DIMENSIONS

PROFILES	PAPER 01	PAPER 02	TOTAL
Computation	18	36	54
Comprehension	24	48	72
Reasoning	18	36	54
Total	60	120	180

### ◆ REGULATIONS FOR PRIVATE CANDIDATES

Candidates who are registered privately will be required to sit Paper 01 and Paper 02. Detailed information on Papers 01 and 02 is given on pages 2 – 4 of this syllabus.

Private candidates must be entered through institutions recognized by the Council.

### ◆ REGULATIONS FOR RESIT CANDIDATES

Resit candidates will be required to sit Paper 01 and Paper 02. Detailed information on Paper 01 and 02 is given on pages 2 - 4 of this syllabus.

Resit candidates must be entered through a school or other approved educational institution.

### ◆ SYMBOLS USED ON THE EXAMINATION PAPERS

The symbols shown below will be used on examination papers. Candidates, however, may make use of any symbol or nomenclature provided that such use is consistent and understandable in the given context. Measurement will be given in S I Units.

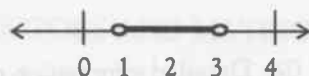
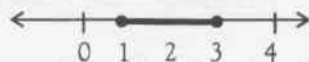
SYMBOL	DEFINITION
<u>Sets</u>	
$U$	universal set
$\{ \} \text{ or } \phi$	the null (empty) set
$\subset$	a subset of
$A'$	complement of set A
$\{x: \dots\}$	the set of all x such that ...

## Relations and Functions and Graphs

$$y \propto x^n$$

$$gf(x)$$

$$g^2(x)$$



$$y \text{ varies as } x^n$$

$$g[f(x)]$$

$$g[g(x)]$$

$$\{x : 1 \leq x \leq 3\}$$

$$\{x : 1 < x < 3\}$$

## Number Theory

W

the set of whole numbers

N

the set of natural (counting) numbers

Z

the sets of integers  $\begin{cases} Z^+ & \text{- positive integers} \\ Z^- & \text{- negative integers} \end{cases}$

Q

the set of rational numbers

R

the set of real numbers

$$5.4\dot{3}2$$

$$5.432\ 432\ 432\ \dots$$

$$9.87\dot{2}1$$

$$9.87212121\ \dots$$

## Measurement

$$05:00\ \text{h.}$$

$$5:00\ \text{a.m.}$$

$$13:15\ \text{h.}$$

$$1:15\ \text{p.m.}$$

$$7\text{mm} \pm 0.5\ \text{mm}$$

$$7\text{mm to the nearest millimetre}$$

$$10\ \text{m/s or } 10\ \text{ms}^{-1}$$

$$10\ \text{metres per second}$$

## Geometry

For transformations these symbols will be used.

M

reflection




$R_\theta$

rotation through  $\theta^\circ$

T

translation



G	glide reflection
E	enlargement
$MR_\theta$	rotation through $\theta$ followed by reflection.
$\angle, \sphericalangle, \wedge$	angle
$\equiv$	is congruent to
	line AB
	ray AB
	line segment AB

### Vectors and Matrices

$\underline{a}$ or $\vec{a}$	vector $\underline{a}$
$\overrightarrow{AB}$	vector AB
$ \overrightarrow{AB} $	magnitude of vector AB
If	$\begin{bmatrix} a & b \\ c & d \end{bmatrix}$ or $\begin{pmatrix} a & b \\ c & d \end{pmatrix}$ is the matrix X
then	$\begin{vmatrix} a & b \\ c & d \end{vmatrix}$ is the determinant of X, written $ X $ or $\det X$ .
$A^{-1}$	inverse of the matrix A
I	identity matrix
O	zero matrix

### Other Symbols

$=$	is equal to or equals
$\geq$	is greater than or equal to
$\leq$	is less than or equal to

$\approx$

is approximately equal to

$\Rightarrow$

implies

$A \Rightarrow B$

if A, then B

$A \Leftrightarrow B$

If A, then B

and

If B, then A

A is equivalent to B

## ◆ FORMULAE AND TABLES PROVIDED IN THE EXAMINATION

Volume of a prism  $V = Ah$  where  $A$  is the area of a cross-section and  $h$  is the perpendicular length.

Volume of cylinder  $V = \pi r^2 h$  where  $r$  is the radius of the base and  $h$  is the perpendicular height.

Volume of a right pyramid  $V = \frac{1}{3} Ah$  where  $A$  is the area of the base and  $h$  is the perpendicular height.

Circumference  $C = 2\pi r$  where  $r$  is the radius of the circle.

Area of a circle  $A = \pi r^2$  where  $r$  is the radius of the circle.

Area of trapezium  $A = \frac{1}{2} (a + b) h$  where  $a$  and  $b$  are the lengths of the parallel sides and  $h$  is the perpendicular distance between the parallel sides.

Roots of quadratic equations If  $ax^2 + bx + c = 0$ ,

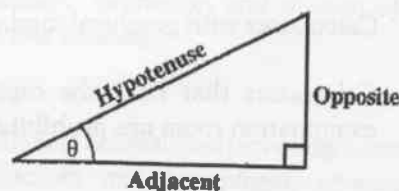
$$\text{then } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Trigonometric ratios

$$\sin \theta = \frac{\text{opposite side}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent side}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite side}}{\text{adjacent side}}$$



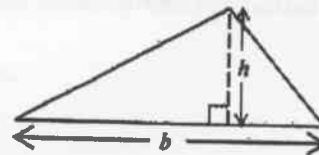
Area of triangle

Area of  $\Delta = \frac{1}{2} bh$  where  $b$  is the length of the base and  $h$  is the perpendicular height

$$\text{Area of } \Delta ABC = \frac{1}{2} ab \sin C$$

$$\text{Area of } \Delta ABC = \sqrt{s(s-a)(s-b)(s-c)}$$

$$\text{where } s = \frac{a+b+c}{2}$$

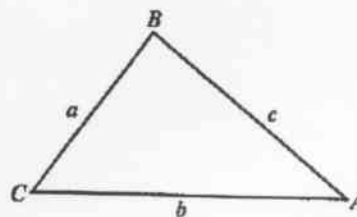


Sine rule

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Cosine rule

$$a^2 = b^2 + c^2 - 2bc \cos A$$



## ◆ USE OF ELECTRONIC CALCULATORS

Candidates are expected to *have* an electronic calculator and are encouraged to use such a calculator in Paper 02.

Guidelines for the use of electronic calculators are listed below.

1. Silent, electronic hand-held calculators may be used.
2. Calculators should be battery or solar powered.
3. Candidates are responsible for ensuring that calculators are in working condition.
4. Candidates are permitted to bring a set of spare batteries in the examination room.
5. No compensation will be given to candidates because of faulty calculators.
6. No help or advice is permitted on the use or repair of calculators during the examination.
7. Sharing calculators is **not** permitted in the examination room.
8. Instruction manuals, and external storage media (for example, card, tape, disk, smartcard or plug-in modules) are **not** permitted in the examination room.
9. Calculators with graphical display, data bank, dictionary or language translation are **not** allowed.
10. Calculators that have the capability of communication with any agency in or outside of the examination room are **prohibited**.

## ◆ SECTION 1 - COMPUTATION

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. *demonstrate* an understanding of place value;
2. *demonstrate* computational skills;
3. be aware of the importance of accuracy in computation;
4. appreciate the need for numeracy in everyday life;
5. *demonstrate the ability to make* estimates fit for purpose.

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

1. perform *computation using* any of the *four* basic operations with real numbers;
2. convert among fractions, percentages and decimals;
3. convert from one set of units to another;
4. express a value to a given number of:
  - (a) significant figures;
  - (b) decimal places;
5. write any rational number in standard form;

Addition, multiplication, subtraction and division of whole numbers, fractions and decimals.

Conversion of fractions to decimals and percentages, conversion of decimal to fractions and percentages, conversion of percentages to decimals and fractions.

Conversion using conversion scales, converting within the metric scales, 12-hour and 24-hour clock, currency conversion.

1, 2 or 3 significant figures.  
1, 2 or 3 decimal places.

Scientific notation.

## COMPUTATION (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

- |     |  |  |
|-----|--|--|
| 6.  | calculate any fraction or percentage of a given quantity;    | <i>Calculating fractions and percentages of a whole.</i>         |
| 7.  | express one quantity as a fraction or percentage of another; | <i>Comparing two quantities using fractions and percentages.</i> |
| 8.  | compare two quantities using ratios;                         | <i>Ratio and proportion.</i>                                     |
| 9.  | divide a quantity in a given ratio;                          | <i>Ratio and proportion.</i>                                     |
| 10. | solve problems involving:                                    |  |
|     | (a) fractions;   |  |
|     | (b) decimals;  |  |
|     | (c) percentages;   |  |
|     | (d) ratio, rates and proportions;                            |  |
|     | (e) arithmetic mean.   |  |

## ◆ SECTION 2 - NUMBER THEORY

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. understand and appreciate the decimal numeration system;
2. appreciate the development of different numeration systems;
3. demonstrate the ability to use rational approximations of real numbers;
4. demonstrate the ability to use number properties to solve problems;
5. develop the ability to use patterns, trends and investigative skills.

### SPECIFIC OBJECTIVES

Students should be able to:

1. distinguish among sets of numbers;
2. order a set of real numbers;
3. generate a term of a sequence given a rule;
4. derive an appropriate rule given the terms of a sequence;
5. identify a given set of numbers as a subset of another set;
6. list the set of factors or a set of multiples of a given positive integer;

### CONTENT

Set of numbers:

natural numbers  $\{1, 2, 3, \dots\}$ , whole numbers  $\{0, 1, 2, 3, \dots\}$ , integers  $\{\dots -2, -1, 0, 1, 2, \dots\}$ , rational numbers  $(\frac{p}{q} : p \text{ and } q \text{ are integers, } q \neq 0)$ , irrational

numbers (numbers that cannot be expressed as terminating or recurring decimals, for example, numbers such as  $\pi$  and  $\sqrt{2}$ ), the real numbers (the union of rational and irrational numbers); sequences of numbers that have a recognizable pattern; factors and multiples; square numbers; even numbers; odd numbers; prime numbers; composite numbers.

Sequences of numbers that have a recognizable pattern.

Sequences of numbers that have a recognizable pattern.

Inclusion relations, for example,  $N \subset W \subset Z \subset Q \subset R$ .

## NUMBER THEORY (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

7. compute the H.C.F. or L.C.M. of two or more positive integers;
8. state the *value* of a digit in a numeral in base  $n$ , where  $n \leq 10$ ;  
*Place value and face value of numbers 2, 3, 4, 5, 6, 7, 8, 9 and 10 in base.*
9. use properties of numbers and operations in computational tasks;  
*Additive and multiplicative identities and inverses, concept of closure, properties of operations such as commutativity, distributivity and associativity, order of operations in problems with mixed operations.*
10. solve problems involving concepts in number theory.



## ◆ SECTION 3 - CONSUMER ARITHMETIC

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. develop the ability to perform the calculations required in normal business transactions, and in computing their own budgets;
2. appreciate the need for both accuracy and speed in calculations;
3. appreciate the advantages and disadvantages of different ways of investing money;
4. appreciate that business arithmetic is indispensable in everyday life;
5. demonstrate the ability to use concepts in consumer arithmetic to describe, model and solve real-world problems.

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

1. calculate discount, sales tax, profit or loss;
2. express a profit, loss, discount, markup and purchase tax, as a percentage of some value;
3. solve problems involving marked price (or selling price), cost price, percentage profit, loss or discount;
4. solve problems involving payments by installments as in the case of hire purchase and mortgages;
5. solve problems involving simple interest,

Principal, time, rate, amount.

## CONSUMER ARITHMETIC (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

6. solve problems involving compound interest, appreciation, and depreciation; Principal, time, rate, amount (not more than 3 periods).
7. solve problems involving measures and money; Include exchange rate.
8. solve problems involving:
  - (a) rates and taxes;
  - (b) utilities;
  - (c) invoices and shopping bills;
  - (d) salaries and wages;
  - (e) insurance and investments.

## ◆ SECTION 4 - SETS

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. demonstrate the ability to communicate using set language and concepts;
2. demonstrate the ability to reason logically;
3. appreciate the importance and utility of sets in analyzing and solving real-world problems.

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

- |  |   |
|--|---|
| 1. explain concepts relating to sets;  | Examples and non-examples of sets, description of sets using words, membership of a set, cardinality of a set, finite and infinite sets, universal set, empty set, complement of a set, subsets.                              |
| 2. represent a set in various forms;   | Listing elements, for example, the set of natural numbers 1, 2 and 3.<br>Set builder notation, for example, $\{x: 0 < x < 4 \text{ where } x \in \mathbb{N}\}$ .<br>Symbolic representation, for example, $A = \{1, 2, 3\}$ . |
| 3. describe relationships among sets using set notation and symbols;                   | Universal, complement, subsets, equal and equivalent sets, intersection, disjoint sets and union of sets.   |
| 4. list subsets of a given set;  | Number of subsets of a set with $n$ elements.   |
| 5. determine elements in intersections, unions and complements of sets;                | Intersection and union of not more than three sets.<br>Apply the result $n(A \cup B) = n(A) + n(B) - n(A \cap B)$ .   |
| 6. construct Venn diagrams to represent relationships among sets;                      | Not more than 3 sets.   |
| 7. solve problems involving the use of Venn diagrams;                                  |   |
| 8. solve problems in Number Theory, Algebra and Geometry using concepts in Set Theory. |   |

## ◆ SECTION 5 - MEASUREMENT

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. *understand that the attributes of an object can be quantified using measurement;*
2. *appreciate that all measurements are approximate and that the relative accuracy of a measurement is dependent on the measuring instrument and the measurement process;*
3. *demonstrate the ability to use concepts in measurement to model and solve real-world problems.*

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

- |   |  |
|---|--|
| 1. calculate the perimeter of a polygon, a circle, and a combination of polygons and circles; | Measures of length, perimeters of polygons and circles.                    |
| 2. calculate the length of an arc of a circle;  |  |
| 3. calculate the area of polygons, a circle and any combination of these;                     | Rectangle, square, parallelogram, trapezium, rhombus and circle.           |
| 4. calculate the area of a sector of a circle;  |  |
| 5. calculate the area of a triangle given two sides and the included angle;                   | Optional Specific Objective.<br>Area of $\Delta = \frac{1}{2} ab \sin C$ . |
| 6. calculate the area of a segment of a circle;   | Optional Specific Objective.   |
| 7. estimate the area of irregularly shaped plane figures;                                     |  |
| 8. calculate the surface area of solids;  | Prism, cylinder, cone, sphere, cube and cuboid.                            |

## MEASUREMENT (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

9. *calculate* the volume of solids; Prism, cylinder, pyramid, cone, sphere, *cube and cuboid*.
10. *convert* units of length, area, capacity, time and speed;
11. *use* the appropriate SI unit of measure for area, volume, mass, temperature and time (24-hour clock) and other derived quantities;
12. *solve* problems involving time, distance and speed;
13. *estimate* the margin of error for a given measurement; Sources of error.  
Maximum and minimum measurements.
14. *use* maps and scale drawings to determine distances and areas;
15. *solve* problems involving measurement.

## ◆ SECTION 6 - STATISTICS

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. appreciate the advantages and disadvantages of the various ways of presenting and representing data;
2. appreciate the necessity for taking precautions in collecting, analyzing and interpreting statistical data and making inferences;
3. demonstrate the ability to use concepts in statistics and probability to describe, model and solve real-world problems.

### SPECIFIC OBJECTIVES

Students should be able to:

1. differentiate between types of data;
2. construct a frequency table for a given set of data;
3. determine class features for a given set of data;
4. construct statistical diagrams;
5. interpret statistical diagrams;
6. determine measures of central tendency for raw, ungrouped and grouped data;
7. determine when it is most appropriate to use the mean, median and mode as the average for a set of data;
8. determine the measures of dispersion (spread) for raw, ungrouped and grouped data;

### CONTENT

Discrete and continuous variables.  
Ungrouped and grouped data.

Ungrouped and grouped data.

Class interval, class boundaries, class limits, class midpoint, class width.

Pie charts, bar charts, line graphs, histograms and frequency polygons.

Pie charts, bar charts, line graphs, histograms and frequency polygons.

Mean, median and mode.

Mean, median and mode as measures of central tendency.

Range, interquartile range and semi-interquartile range.

## STATISTICS (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

9. *construct* a cumulative frequency table for ungrouped and grouped data;
  10. *draw* cumulative frequency curve (Ogive);
  11. *use statistical diagrams*;
  12. *determine* the proportion or percentage of the sample above or below a given value from raw data, table or cumulative frequency curve;
  13. *identify* the sample space for sample experiment;
  14. *determine* experimental and theoretical probabilities of events;
  15. *make inference(s)* from statistics.
- Appropriate scales for axes.  
Class boundaries as domain.
- Mean, mode, median, quartiles range, interquartile range, semi-interquartile range.
- Set of all possible outcomes.
- Raw data, tables, diagrams.

## ◆ SECTION 7 - ALGEBRA

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. appreciate the use of algebra as a language and a form of communication;
2. appreciate the role of symbols and algebraic techniques in solving problems in mathematics and related fields;
3. demonstrate the ability to reason with abstract entities.

### SPECIFIC OBJECTIVES

Students should be able to:

1. use symbols to represent numbers, operations, variables and relations;
2. translate statements expressed algebraically into verbal phrases;
3. perform arithmetic operations involving directed numbers;
4. perform the four basic operations with algebraic expressions;
5. substitute numbers for algebraic symbols in simple algebraic expressions;
6. perform binary operations (other than the four basic ones);
7. apply the distributive law to factorize or expand algebraic expressions;

### CONTENT

Symbolic representation.

For example,  $x(a+b) = xa+xb$  and  $(a+b)(x+y) = (a+b)x + (a+b)y = ax+bx+ay+by$ .



## ALGEBRA (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

8. simplify algebraic fractions;
9. use the laws of indices to manipulate expressions with *integral* indices;
10. solve linear equations in one unknown;
11. solve simultaneous linear equations, in two unknowns, algebraically;
12. solve a simple linear inequality in one unknown;
13. change the subject of formulae; Including those involving roots and powers.
14. factorize algebraic expressions;  $a^2 - b^2$ ;  $a^2 \pm 2ab + b^2$   
 $ax + bx + ay + by$   
 $ax^2 + bx + c$  where  $a, b$ , and  $c$  are integers and  $a \neq 0$
15. solve quadratic equations;
16. solve word problems; Linear equation, Linear inequalities, two simultaneous linear equations, quadratic equations.
17. solve a pair of equations in two variables when one equation is quadratic or non-linear and the other linear; *Optional Specific Objective.*
18. prove two algebraic expressions to be identical;
19. represent direct and indirect variation symbolically;
20. solve problems involving direct variation and inverse variation.

## ◆ SECTION 8 - RELATIONS, FUNCTIONS AND GRAPHS

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. appreciate the importance of relations in Mathematics;
2. appreciate that many mathematical relations may be represented in symbolic form, tabular or pictorial form;
3. appreciate the usefulness of concepts in relations, functions and graphs to solve real-world problems.

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

- |   |  |
|---|--|
| 1. explain concepts associated with relations;                | Concept of a relation, types of relation, examples and non-examples of relations, domain, range, image, co-domain.                   |
| 2. represent a relation in various ways;                      | Set of ordered pairs, arrow diagrams, graphically, algebraically.  |
| 3. state the characteristics that define a function;          | Concept of a function, examples and non-examples of functions.   |
| 4. use functional notation;                                   | For example $f: x \rightarrow x^2$ ; or $f(x) = x^2$ as well as $y = f(x)$ for given domains.  |
| 5. distinguish between a relation and a function;             | Ordered pairs, arrow diagram, graphically (vertical line test).  |
| 6. draw and interpret graphs of linear functions;             | Concept of linear function, types of linear function ( $y = c$ ; $x = k$ ; $y = mx + c$ ; where $m$ , $c$ and $k$ are real numbers). |
| 7. determine the intercepts of the graph of linear functions; | $x$ -intercepts and $y$ -intercepts, graphically and algebraically.  |
| 8. determine the gradient of a straight line;                 | Concept of slope.  |

## RELATIONS, FUNCTIONS AND GRAPHS (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

9. determine the equation of a straight line;  
The graph of the line.  
The co-ordinates of two points on the line.  
The gradient and one point on the line.  
The gradient on the line and its relationship to another line.
10. solve problems involving the gradient of parallel and perpendicular lines;
11. determine from co-ordinates on a line segment:  
The concept of magnitude or length, concept of midpoint.
  - (a) the length;
  - (b) the co-ordinates of the midpoint;
12. solve graphically a system of two linear equations in two variables;
13. represent the solution of linear inequalities in one variable using:
  - (a) set notation;
  - (b) the number line;
  - (c) graph;
14. draw a graph to represent a linear inequality in two variables;

## RELATIONS, FUNCTIONS AND GRAPHS (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

- |     |   |  |
|-----|---|--|
| 15. | use linear programming techniques to solve problems involving two variables;  | <i>Optional Specific Objective.</i>  |
| 16. | derive composite functions;   | Composite function, for example, $fg, f^2$ given $f$ and $g$ .<br><br>Non-commutativity of composite functions ( $fg \neq gf$ ). |
| 17. | state the relationship between a function and its inverse;  | The concept of the inverse of a function.  |
| 18. | derive the inverse of a function;   | $f^{-1}, (fg)^{-1}$  |
| 19. | evaluate $f(a), f^{-1}(a), fg(a), (fg)^{-1}(a)$ ;   | Where $a \in \mathbb{R}$ .   |
| 20. | use the relationship $(fg)^{-1} = g^{-1}f^{-1}$ ;   | The concept of the inverse of a function, determining the inverse of a given function.   |
| 21. | draw and interpret graphs of a quadratic function to determine:<br><br>(a) the elements of the domain that have a given image;<br><br>(b) the image of a given element in the domain;<br><br>(c) the maximum or minimum value of the function;<br><br>(d) the equation of the axis of symmetry; | Concepts of gradient of a curve at a point, tangent, turning point. Roots of the equation.                                       |

## RELATIONS, FUNCTIONS AND GRAPHS (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

*draw and interpret graphs of a quadratic function to determine: (cont'd)*

- (e) *the interval of the domain for which the elements of the range may be greater than or less than a given point;*
  - (f) *an estimate of the value of the gradient at a given point;*
  - (g) *intercepts of the function;*
22. *determine the axis of symmetry, maximum or minimum value of a quadratic function expressed in the form  $a(x + h)^2 + k$ ;*
23. *sketch graph of quadratic function expressed in the form  $a(x+h)^2 + k$  and determine number of roots;*
24. *draw and interpret the graphs of other non-linear functions;*
25. *draw and interpret distance-time graphs and speed-time graphs (straight line only) to determine:*
- (a) *distance;*
  - (b) *time;*
  - (c) *speed;*
  - (d) *magnitude of acceleration.*

**Optional Specific Objective.**

**Optional Specific Objective.**

**Optional Specific Objective.**  
 $y = ax^n$  where  $n = -1, -2$  and  $+3$ .

**Optional Specific Objective.**

## ◆ SECTION 9 - GEOMETRY AND TRIGONOMETRY

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. *appreciate the notion of space as a set of points with subsets of that set (space) having properties related to other mathematical systems;*
2. *understand the properties and relationship among geometrical objects;*
3. *understand the properties of transformations;*
4. *demonstrate the ability to use geometrical concepts to model and solve real world problems;*
5. *appreciate the power of trigonometrical methods in solving authentic problems.*

### SPECIFIC OBJECTIVES

Students should be able to:

1. *explain* concepts relating to geometry;
2. *draw and measure* angles and line segments accurately using appropriate geometrical instruments;
3. *construct* lines, angles, and polygons using appropriate geometrical instruments;
4. *identify* the type(s) of symmetry possessed by a given plane figure;
5. *solve* geometric problems using properties of:
  - (a) lines, angles, and polygons;
  - (b) circles;

### CONTENT

Point, line, parallel lines, intersecting lines and perpendicular lines, line segment, ray, curve, plane, angle (acute, reflex, right angle, straight angle), face, edge, vertex.

Parallel and perpendicular lines.  
Triangles, quadrilaterals, regular and irregular polygons.  
Angles to be constructed include 30, 45, 60, 90, 120.

Line(s) of symmetry, rotational symmetry, order of rotational symmetry.

Vertically opposite angles, alternate angles, adjacent angles, corresponding angles, co-interior angles, angles at a point, complementary angles, supplementary angles. Parallel lines and transversals. Equilateral, right, and isosceles triangles. Square, rectangle, rhombus, kite, parallelogram, trapezium.

## GEOMETRY AND TRIGONOMETRY (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

solve geometric problems using properties of: (cont'd)

- |   |  |
|---|--|
| <ul style="list-style-type: none"> <li>(c) congruent triangles;</li> <li>(d) similar figures;</li> <li>(e) faces, edges and vertices of solids;</li> <li>(f) classes of solids;</li> </ul>        | <p>Prisms, pyramids, cylinders, cones, sphere.</p>   |
| <p>6. represent translations in the plane using vectors;</p>  | <p>Column matrix notation <math>\begin{pmatrix} x \\ y \end{pmatrix}</math>.</p>   |
| <p>7. determine and represent the location of :</p> <ul style="list-style-type: none"> <li>(a) the image of an object ;</li> <li>(b) an object given the image under a transformation;</li> </ul> | <p>A <i>translation</i> in the plane; a <i>reflection</i> in a line in that plane; a <i>rotation</i> about a point (the centre of rotation) in that plane; an <i>enlargement</i> or <i>reduction</i> in that plane.</p>                                |
| <p>8. identify the relationship between an object and its image in the plane after a geometric transformation;</p>  | <p>Similar; Congruent.</p>   |
| <p>9. describe a transformation given an object and its image;</p>  | <p>A <i>translation</i> in the plane; a <i>reflection</i> in a line in that plane; a <i>rotation</i> about a point (the centre of rotation) through an angle in the plane; an <i>enlargement</i> or <i>reduction</i> in that plane about a center.</p> |
| <p>10. locate the image of a set of points under a combination of transformations;</p>  | <p>Combination of any two of enlargement/reduction, translation, rotation, reflection, glide reflection.</p>   |
| <p>11. state the relations between an object and its image as the result of a combination of two transformations;</p>   |  |

## GEOMETRY AND TRIGONOMETRY (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

12. use Pythagoras' theorem to solve problems;
13. *determine* the trigonometric ratios of acute angles in a right-angled triangle;
14. use trigonometric ratios in the solution of right angled-triangles;
15. use trigonometric ratios to solve problems based on measures in the physical world;
16. use the sine and cosine rules in the solution of problems involving triangles;
17. *represent* the relative position of two points given the bearing of one point with respect to the other;
18. *determine* the bearing of one point relative to another point given the position of the points.
19. solve problems involving bearings;
20. solve practical problems involving heights and distances in three dimensional situations;

Practical geometry and scale drawing, bearing.

Heights and distances; angles of elevation and depression.

**Optional Specific Objective.**



## GEOMETRY AND TRIGONOMETRY (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

21. solve geometric problems using properties of circles and circle theorems.

*The angle which an arc of a circle subtends at the centre of a circle is twice the angle it subtends at any point on the remaining part of the circumference.*

*The angle in a semicircle is a right angle.*

*Angles in the same segment of a circle and subtended by the same arc are equal.*

*The opposite angles of a cyclic quadrilateral are supplementary.*

*The exterior angle of a cyclic quadrilateral is equal to the interior opposite angle.*

*A tangent of a circle is perpendicular to the radius of that circle at the point of contact.*

*The lengths of two tangents from an external point to the points of contact on the circle are equal.*

*The angle between a tangent to a circle and a chord through the point of contact is equal to the angle in the alternate segment.*

*The line joining the centre of a circle to the midpoint of a chord is perpendicular to the chord.*

## ◆ SECTION 10 - VECTORS AND MATRICES

### GENERAL OBJECTIVES

On completion of this Section, students should:

1. demonstrate the ability to use vector notation and concepts to model and solve real-world problems;
2. develop awareness of the existence of certain mathematical objects, such as matrices, that do not satisfy the same rules of operation as the real number system;
3. demonstrate how matrices can be used to represent certain types of linear transformation in the plane.

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

1. explain concepts associated with vectors;  
Concept of a vector, magnitude, direction, line segment, scalar.
2. combine vectors;  
Triangle law, or parallelogram laws  
2x1 Column matrices,  
for example,  $\begin{pmatrix} a \\ b \end{pmatrix} + \begin{pmatrix} c \\ d \end{pmatrix} = \begin{pmatrix} a+c \\ b+d \end{pmatrix}$   
Vector algebra.
3. express a point  $P(a,b)$  as a position vector  
 $\vec{OP} = \begin{pmatrix} a \\ b \end{pmatrix}$   
where O is the origin (0, 0);  
Displacement and position vectors; co-ordinates.
4. determine the magnitude of a vector;  
Including unit vectors.
5. use vectors to solve problems in Geometry;  
Collinearity, parallel.
6. explain concepts associated with matrices;  
Concept of a matrix, row, column, order, types of matrices, practical use.

## VECTORS AND MATRICES (cont'd)

### SPECIFIC OBJECTIVES

### CONTENT

Students should be able to:

7. *perform* addition, subtraction and multiplication of matrices and multiplication of matrices by a scalar; Non-commutativity of *matrix multiplication*.
8. *evaluate* the determinant of a '2 x 2' matrix;
9. *solve* problems involving a '2 x 2' singular matrix;
10. obtain the inverse of a non-singular '2 x 2' matrix; *Determinant and adjoint of a matrix.*
11. *determine* a '2 x 2' matrix associated with specified transformations;
12. *determine* a '2 x 2' matrix representation of the single transformation which is equivalent to the composition of two linear transformations in a plane (where the origin remains fixed);
13. *use* matrices to solve simple problems in *Arithmetic, Algebra and Geometry*. Use of matrices to solve linear simultaneous equations. (Matrices of order greater than '3 x 3' will not be set.)

## ◆ **RECOMMENDED TEXTS**

Buckwell, G., Solomon, R., and Chung Harris, T.

Chandler, S., Smith, E., Ali, F., Layne, C. and Mothersill, A.

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Toolsie, R.

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*CXC Mathematics for Today 1*, Oxford: Macmillan Education, 2005.

*Mathematics for CSEC*, United Kingdom: Nelson Thorne Limited, 2008.

*Mathematics for the Caribbean 4*, Oxford: Oxford University Press, 2006.

*Certificate Mathematics, A Revision Course for the Caribbean*, United Kingdom: Nelson Thorness Limited, 2001.

*STP Caribbean Mathematics for CXC Book 4*, United Kingdom: Nelson Thorness Limited, 2005.

*Mathematics, A Complete Course Volume 1*, Caribbean Educational Publisher Limited, 2006.

*Mathematics, A Complete Course Volume 2*, Caribbean Educational Publisher Limited, 2006.

### Websites

<http://mathworld.wolfram.com/>

<http://plus.maths.org/>

<http://nrich.maths.org/public/>

<http://mathforum.org/>

<http://www.ies.co.jp/math/java/>